

# Advanced topics in algorithms:

bibliography list 4

Here are the reference on algorithms for Maximum flows on planar graphs. It started with Itai and Shiloach [6]. Reif improved their method for finding a minimum cut [8]. Hassin [4] gave a very simple algorithm for maximum flow in  $s - t$  planar graphs (meaning that  $s$  and  $t$  are on the boundary of the same face). More early results can be found in [7, 5]. The new algorithm for directed graphs is by Borradaile and Klein [1]. A simpler presentation was given by Erickson [3]. The extension to multiple sources and sinks is in [2].

## References

- [1] Glencora Borradaile and Philip Klein. An  $O(n \log n)$  algorithm for maximum  $st$ -flow in a directed planar graph. *J. ACM*, 56(2):1–30, 2009.
- [2] Glencora Borradaile, Philip N. Klein, Shay Mozes, Yahav Nussbaum, and Christian Wulff-Nilsen. Multiple-source multiple-sink maximum flow in directed planar graphs in near-linear time. In *IEEE 52nd Annual Symposium on Foundations of Computer Science (FOCS)*, pages 170–179, 2011.
- [3] J. Erickson. Maximum flows and parametric shortest paths in planar graphs. In *21st SODA*, pages 794–804, 2010.
- [4] R. Hassin. Maximum flows in  $(s, t)$  planar networks. *IPL*, page 107, 1981.
- [5] Refael Hassin and Donald B. Johnson. An  $O(n \log^2 n)$  algorithm for maximum flow in undirected planar networks. *SIAM J. Comput.*, 14(3):612–624, 1985.
- [6] Alon Itai and Yossi Shiloach. Maximum flow in planar networks. *SIAM Journal on Computing*, 8(2):135–150, 1979.
- [7] S. Khuller, J. Naor, and P. Klein. The lattice structure of flow in planar graphs. 6(3):477–490, 1993.
- [8] J. Reif. Minimum  $s-t$  cut of a planar undirected network in  $O(n \log^2 n)$  time. *SIAM Journal on Computing*, 12:71–81, 1983.