Neuronal Regulation vs Synaptic Unlearning in Memory Maintenance Mechanisms

David Horn and Nir Levy School of Physics and Astronomy Tel Aviv University, Tel Aviv 69978, Israel and Eytan Ruppin

Departments of Computer Science & Physiology Tel Aviv University, Tel Aviv 69978, Israel

April 21, 1998

Abstract

Hebbian learning, the paradigm of memory formation, needs further mechanisms to guarantee creation and maintenance of a viable memory system. One such additional mechanism is Hebbian unlearning, a process hypothesized to occur during sleep. It can remove spurious states and eliminate global correlations in the memory system. The problem of spurious states is unimportant in the biologically interesting case of memories that are sparsely coded on excitatory neurons. Moreover, if some memories are anomalously strong and have to be weakened to guarantee proper functioning of the network, we show that it is advantageous to do that by neuronal regulation (NR) rather than synaptic unlearning. Neuronal regulation leads to dynamical maintenance of memory systems that undergo continuous synaptic turnover. This neuronal based mechanism, regulating all excitatory synapses according to neuronal average activity, has recently gained strong experimental support. NR achieves synaptic maintenance over short time scales by preserving the average neuronal input field. On longer time scales it acts to maintain memories by letting the stronger synapses grow to their upper bounds. In aging, NR further increases the synaptic values to overcome the loss of synaptic degredation.

1 Introduction

In a recent viewpoint article, van Hemmen[1] has reviewed problems caused by Hebbian learning in some memory models, and the unlearning method that resolves them. Unlearning, in this context, is the idea of applying Hebbian learning with a reversed sign to undesired states, such as spurious mixed states in a Hopfield model[2]. This idea was put forward in 1983 by Crick and Mitchison[3] and by Hopfield, Feinstein and Palmer[4]. In his review paper, van Hemmen discusses the motivation of this approach and describes the reasons for its success. He puts unlearning in the larger context of eliminating undesirable global correlations between memories and performs thorough simulations to substantiate the theory. Nonetheless the simulations cannot be extended to the biologically interesting case of low coding. Moreover, the problem of spurious states is absent in models of sparse coding.

The one situation that may need a cure of an unlearning type is the case of pathologic attractors[5, 6]. This concept refers to memories in an associative memory model, that possess anomalously large basins of attraction. An associative memory system that performs free recall from random stimuli, and then learns in a Hebbian fashion the memories it recalls, can fall into a pathologic behavior in which some basins of attraction grow exponentially and overshadow all other memories. Obviously this should be avoided in functional memory systems.

We have found a cure for the problem of pathologic attractor formation while trying to address a completely different problem, namely, the question how can memories be maintained for long time in the face of continuous metabolic turnover of synapses. We have presented[7] a novel solution based on a **neuronal regulation** (NR) mechanism that acts to maintain neuronal activity. This mechanism operates in conjunction with random activation of the memory system, and is able to counterbalance degradation of synaptic weights. At the same time, it normalizes basins of attraction of memories, thus preventing the creation of pathologic attractors.

Activity-dependent neural regulatory processes have been previously observed experimentally[8] and studied theoretically[9, 10]. The main new feature introduced in our work is the view of NR as a common change in the synaptic efficacies of a neuron that, depending on the neuron's activity, keeps the relative weights of different synapses unchanged. This key feature has recently received direct experimental support from the work of Turrigiano et al. [11], showing that neocortical pyramidal neurons regulate their firing rates by scaling the strength of their synaptic connections up or down as a function of activity. This is a slow process, affecting AMPA-type receptors that mediate excitatory synaptic transmission. Just as in the model[7], it produces long-lasting regulation in the desired multiplicative post-synaptic fashion.

In Section 2 we briefly describe our model. We show that there exists an analogy between NR and unlearning, as both mechanisms weaken memories that are too strongly retrieved. However, in contradistinction to unlearning, NR does not involve an anti-Hebbian synaptic mechanism. Instead, it employs a neuronal mechanism, acting simultaneously on all its dendritic synapses. This mechanism cohabitates harmoniously with Hebbian learning, and ensures homeostasis of memory systems.

Section 3 is devoted to long term maintenance, when synapses are no longer kept at their original values, nonetheless memories can be maintained in tact. In Section 4 we review pathologies that arise when neuronal regulation fails (dementia) or when it acts under wrong conditions, as in a model of schizophrenia. We contrast the achievements of NR with the results of synaptic unlearning in Section 5, and end with a discussion in Section 6 that is mainly devoted to the possible implementation of NR in sleep.

2 Neuronal Regulation

2.1 Short Term Maintenance

As a platform for the formulation and testing of our approach we use the neural network model of Tsodyks[13], taking it to represent a module of associative cortex in which a set of memories is engraved. The model includes N excitatory neurons that encode M memory patterns with sparse coding level $p \ll 1$. The effect of inhibitory neurons is represented by global inhibition that is proportional to the overall activity of the excitatory neurons. The conventional Hebbian approach specifies an increase in the synaptic weight J_{ij} , projecting from neuron j to neuron i, in terms of the product of the joint activities of these two neurons when a new memory is encoded. Thus, the synaptic weight matrix, after the consecutive storage of M memory patterns η^{μ} , becomes

$$J_{ij} = \frac{1}{Np} \sum_{\mu=1}^{M} \eta_i^{\mu} \eta_j^{\mu}.$$
 (1)

The dynamics of retrieval is given by

$$V_i(t' + \Delta t') = \mathcal{S} \left(h_i(t') - T \right) \tag{2}$$

where V_i is the activity of the *i*th binary neuron, t' denotes the fast time scale of network updating in a single retrieval trial, and T is the threshold. S(x) is a stochastic sigmoid function, getting the value 1 with probability $(1 + e^{-x})^{-1}$ and 0 otherwise, and

$$h_{i}(t') = h_{i}^{e}(t') - \frac{\gamma}{Np} \sum_{j}^{N} V_{j}(t') + I_{i}$$
(3)

is the membrane potential. It includes the excitatory Hebbian coupling of all other excitatory neurons,

$$h_i^e(t') = \sum_{j \neq i}^N J_{ij} V_j(t') \tag{4}$$

an external input I_i , and inhibition that is proportional to the total activity of the excitatory neurons.

In the model the synaptic weight matrix undergoes two types of changes. One is $J_{ij} \rightarrow (1 - \epsilon_{ij})J_{ij}$, due to synaptic turnover, represented here by a deterioration factor ϵ_{ij} that is synapse specific and is newly chosen at every deterioration cycle in a random fashion (with mean ϵ and variance σ^2). The second type of change is the NR effect, multiplying each synaptic weight at every NR cycle by $J_{ij} \rightarrow c_i J_{ij}$. Note that this corrective action is neuron specific, i.e. c_i is determined by the post-synaptic neuron i, multiplying all the synapses on the dendritic tree of neuron i by the same factor. c_i itself is chosen to be slightly larger (or smaller) than 1, according to whether the average input seen by neuron i in the NR cycle is weaker (or stronger) than a specified baseline value. This is the same type of regulation as has been recently observed experimentally [11]. The definition of c is given by

$$c_{i} = 1 + \tau \tanh\left[\kappa \left(1 - \frac{\langle h^{e}_{i}(t) \rangle}{H_{i}^{e}}\right)\right]$$
(5)

where $H_i^e = \langle h^e{}_i(t=0) \rangle$ and κ and τ are rate constants.

The NR mechanism can counter-balance the average deterioration of the system, and works nicely as long as the accumulated variance is small. We have run it[7] on a system that undergoes consecutive cycles of Hebbian learning, synaptic degradation and neuronal regulation and found that it performs very well, maintaining both old and new memories, and storing all of them with roughly the same strength, i.e. similar basins of attraction.

In our calculations we have to make a clear distinction between Hebbian learning and neuronal regulation periods. In Nature we assume that the two correspond to different modes of activity in the brain. As already stated above, the Hebbian process modifies the single synapse, based on the activity of both pre- and post-synaptic neurons, whereas the NR mechanism modifies all synapses of the (post-synaptic) neuron based on its average activity. To measure this average activity, random excitations of the memory system are invoked and hence learning cannot take place during this stage. These random activations, in turn, evoke many memories, thus activating every neuron. This activity indicates to each neuron the size of its overall synaptic degradation, on which it can base its appropriate corrective measure c_i .

2.2 Experimental Evidence

The recent results of [11] point out an experimental behavior which is very much in the spirit of the NR model outlined above. They show that blocking the activity of a cortical culture, the amplitude of miniature postsynaptic currents (mEPSCs) increases. If, on the other hand, inhibition is blocked, thus increasing the activity, the mEPSC amplitudes will decrease until firing rates return to baseline values. Thus, the neuron is able to keep its

firing rate at a steady-state value irrespective of external input changes. This works through up or down regulation of excitatory AMPA-type receptors. Moreover, it is a multiplicative effect, just as expected from the neuronal regulation factor of Eq. (5). This type of synaptic plasticity was observed over periods of up to 48 hours. We may thus conclude that NR and Hebbian learning are two different synaptic modification mechanisms: NR is a slow, neuronspecific process that directly modifies AMPA-mediated conductance, while Hebbian learning (i.e., LTP/LTD) is carried out by fast, NMDA-dependent synapse-specific processes.

Homeostatic mechanisms controlling synaptic efficacies were also recently reported by [14]. Working on genetically manipulated muscle innervation in the *Drosophila* they have observed a compensatory change in quantal size at the neuromuscular junction that is anticorrelated with the increase or decrease of the innervation, as would be expected from the action of NR processes. In addition there exists evidence[15] that during the formation of the neuromuscular junction weak synapses are eliminated while stronger ones are retained. This is in agreement with our ideas concerning long term maintenance that are discussed in Section 3.

We view all these results as experimental evidence for homeostatic regulation of neuronal activity. Within our model we make additional assumptions that are, so far, still speculative: When applying NR to an associative memory model we assume that there exist periods of random activation that are being used by the system to estimate the average excitatory field and take the required corrective measures. How this is taking place, and if this is indeed connected to sleep (as was previously suggested[3, 4] for random activation in unlearning) is still an open question.

2.3 Normalization of Basins of Attraction

Homeostasis of neuronal baseline activity has an interesting consequence for an associative memory model. If all neurons have a similar baseline it follows also that all memories have a similar basin of attraction since, if this would not be the case, some neurons that belong to the stronger memories would be more active than others. To demonstrate this property we display in Fig. 1 a case of 50 memories, few of which start out with different basins of attraction because their coding level p is less sparse than that of the rest. Note that van-Hemmen[1] points out the difficulty of unlearning and homogenizing the basins of attraction in such a situation of mixed coding levels. In our model this poses no problem, and the basins of attraction homogenize as NR is being activated.



Figure 1: Regulation of the size of basins of attraction with mixed coding levels. In this simulation of M = 50 memories in a system of N = 1000 neurons some of the memories have different coding levels. This system undergoes synaptic degradation and NR cycles, without any Hebbian learning, leading to homogenization of the basins of attraction. The different symbols refer to the leading memories and to the null-attractor. The latter is the only attractor in this system other than the memories. It corresponds to the state of total quiescence. Its basin of attraction grows and then diminishes as the process continues. After 200 simulation steps the basins of attraction of the memories are much more homogeneous than at the start.

We find this property to be particularly important since it explains how one may avoid the creation of pathologic attractors. It allows one to train an associative memory model using different memory strengths and durations during the Hebbian paradigm, and let the NR phase regulate the result into a homogeneous and well balanced memory system.

3 Long Term Maintenance

Synaptic maintenance by NR fails if the variance of synaptic deterioration becomes too strong. Even if each deterioration step has small variance, the cumulative variance will increase with time leading eventually to the demise of the system. Thus one may define a critical time [7], that decreases rapidly with increasing σ , beyond which the spread of the synaptic weights that arises from the deterioration process becomes so wide that the system loses its memories. There exists, however, a remedy to this problem: putting an upper bound on synaptic weights. This is displayed in Fig. 2, where we test a system with large variance of synaptic degradation, that causes fast deterioration in memory retrieval performance unless synapses are appropriately bounded. We find [7] that, for appropriate synaptic upper bounds, the network may successfully maintain its stored memories forever even in face of ongoing, continuous, synaptic turnover. The simple intuitive explanation is that by letting the degradation-maintenance process continue for a long time the synapses undergo a random walk process with bounds. If the synaptic bound is sufficiently low, the number of large synapses retained by the NR mechanism will be higher than the minimal number of synapses required to maintain memory performance. By maintaining the neurons' average post-synaptic potentials, the NR mechanism preserves the number of large synapses practically forever, even though the identity of these synapses may change during the network's life-time.

The possibility that the network can achieve stability, i.e. that it continues to exhibit high retrieval performance forever, is further enhanced when a 'viability' bound is incorporated. In this case, synapses whose values decrease below some lower bound die and their values are set to zero. This NR induced selective synaptic death process helps pre-



Figure 2: The effect of synaptic bounds. The small circles denote the performance of the network without synaptic bounds. The '+' symbols denote the performance of the network with an upper bound of 8/Np (i.e., 8 times the size of a synapse that stores one memory at t = 0), while the '*' symbols correspond to an upper bound of 3/Np. The other parameters of the simulation are N = 500, M = 25, p = 0.075, $\epsilon = 0.005$, $\sigma = 0.2$. For further details see [7].

serve the network's performance because synapses with large initial values (i.e., synapses that encode several memories) have greater chances to survive than synapses with small initial values. The former are clearly more significant. This intuitive notion, supported by the work of Sompolinsky[16] on clipped synapses, has recently been proven formally by Chechick *et al.* [17].

4 Neuronal Regulation and its Failure in the Aging and the Ailing Brain

The regular synaptic turnover processes take a turn for the worse in the aging brain, which has to cope with synaptic deletion, a considerable synaptic loss in various cortical regions. NR in this case is manifested by an increase of the synaptic size reflecting a functional compensatory increase of synaptic efficacy [18, 19, 20]. The combined outcome of these counteracting synaptic degenerative and compensatory processes can be evaluated by measuring the total synaptic area per unit volume (TSA). The latter correlates strongly with cognitive ability. For patients of Alzheimer's disease one finds that the TSA decreases as the disease progresses [19, 21, 22, 23], pointing to the important role that pathological synaptic changes play in the cognitive deterioration of AD patients.

This raises the interesting possibility that disturbances of NR mechanisms may underlie the clinical manifestations of Alzheimer's disease [24], explaining the onset of dementia. In the model of [24] a fraction d_i of the input synapses to each neuron i are deleted, and are compensated for by a factor c_i which each neuron adjusts individually. This is equivalent to performing the replacement $J_{ij} \to c_i w_{ij} J_{ij}$ where w_{ij} is either 0 or 1, and $\sum_j w_{ij}/N = 1 - d_i$. The local compensatory factor c_i is determined via neuronal regulation, which keeps the membrane potential and neural activity at their original, premorbid levels. That is, NR must now compensate for the accumulative deletion of synapses. Our working hypothesis was that NR based synaptic compensatory mechanisms, that in normal aging succeed in preserving a considerable level of cognitive functioning, are disrupted in AD. Numerical simulations have allowed us to study the network's performance at various NR (compensation) rates. The performance level is better maintained if the compensation rate is high. As reviewed in [25], young and very old AD patients suffer from rapid clinical deterioration, while the majority of AD patients have a more gradual pattern of decline. These clinical patterns may arise because very old patients have almost no compensation resources and young patients have very potent synaptic compensation mechanisms. Interestingly, studies of reactive synaptogenesis following experimental hippocampal deafferentation lesions in rodents show that the rate of compensatory synaptogenesis decreases as a function of age [26, 27].

Interestingly, not only deficient NR mechanisms may cause pathology. Our modeling studies have shown that even if the NR mechanisms are intact, pathologies may arise if the system in which they operate changes in a way that the mechanism was not designed to control. In [6] we studied a computational model of Stevens' theory of the pathogenesis of schizophrenia [28]. This theory hypothesizes that the onset of schizophrenia is associated with reactive synaptic regeneration occurring in frontal regions receiving degenerating temporal lobe projections. These synaptic changes are modeled in the framework of a "frontal" associative memory network whose internal synapses are strengthened in response to weakened input synapses representing incoming temporal projections. Superimposed on these alterations, we incorporated an enhancement of activity-dependent synaptic changes, to model the hypothesized effects of increased dopaminergic activity observed in schizophrenia (see [6] for more details). As a result of these alterations, the network begins to spontaneously retrieve memory patterns even in the absence of any input retrieval cues, as demonstrated in Fig. 3. This figure traces the distribution of the memory patterns to which the network has spontaneously converged after the assumed pathological alterations are induces. The total frequency of convergence to memory patterns increases as time evolves. As evident, the distribution of the memory patterns spontaneously retrieved tends to concentrate on a single memory pattern as more trials occur. Although the synaptic matrix was initially non-biased, small, random correlations between the network's initial states and a few of the memory patterns are sufficient to overwhelmingly and "pathologically" enhance their retrieval. We therefore see that biased retrieval is formed, and out of the many patterns stored in the network only very few are actually spontaneously retrieved. This pathologic attractor formation of biased spontaneous retrieval can account for the occurrence of schizophrenic delusions and hallucinations without any apparent external trigger, and for their tendency to concentrate on a few central cognitive and perceptual themes. The model presented in [6] also explains why schizophrenic positive symptoms tend to wane as the disease progresses, why delayed therapeutical intervention leads to a much slower response, and why delusions and hallucinations may persist for a long duration.

The demonstration of pathologic attractor formation in schizophrenia points to the



Figure 3: Distribution of spontaneous memory retrieval. The positive feedback that comes about from regulatory compensation, Hebbian learning and random activation, leads to the emergence of pathologic attractors. The x-axis enumerates the memories stored, and the y-axis denotes the retrieval frequency of each memory. For details see [6].

importance of preventing the latter in normal processing. This protective task is probably carefully regulated, and depends on a rather delicate balance between neuronal regulation and the level of activity-dependent synaptic changes (i.e., synaptic plasticity and learning). It further emphasizes the importance of keeping neuronal regulation and learning segregated. If random activation of memories is combined with Hebbian learning it leads to a positive feedback loop that ends up with pathologic attractors.

The possible involvement of NR in both AD and schizophrenia can explain the age difference in the appearance of these disorders. Elderly people are more likely to suffer from decreased compensatory resources and NR dysfunction and hence AD is typically a disease of the old-aged. In contradistinction, in response to a pathologic disconnection between various cortical regions, normal functioning NR can lead to the emergence of spontaneous activation of cortical networks and to the subsequent formation of pathologic attractors. In fact, ailing NR mechanisms will fail to cause spontaneous cortical activation, explaining why schizophrenia (more specifically, its psychotic, positive, symptoms) is typically a disorder of the young.

5 Neuronal Regulation vs Synaptic Unlearning

Both Hebbian unlearning and neuronal regulation were proposed as complementary mechanisms to Hebbian learning. In this Section we wish to compare the two methods.

• Originally, [3, 4] have suggested that unlearning serves to eliminate spurious attractor states and thus increase the memories' basins of attraction. However, while spurious states are abundant in the Hopfield model, they occupy a small and practically negligible fraction of the retrieval scene of the more biologically realistic low-coding memory networks (e.g., [7]). Hence the proposed cure is unwarranted. • As proposed by van Hemmen's work, by eliminating global correlations unlearning may serve to store many patterns with varying activities. As shown here, NR may serve the same goal by homogenizing the basins of attraction of patterns with mixed coding levels (Fig. 1).

It is helpful to distinguish between the issues of reducing global correlations and storing patterns with different activity levels. As noted by van Hemmen himself[1], for low-coding values typical of biological networks, the overlaps between different patterns are much smaller than those manifested in the range of coding levels used by him. Thus, reducing global correlations may not be a real problem. With regard to the second issue, it may well be that both unlearning and NR are insufficient for efficient storage of memories with coding levels that differ by an order of magnitude. For this task, we have recently shown[29] that a multi-modular network is clearly advantageous. Its architecture is based on segregation between inter-modular synaptic couplings and intramodular ones, with the latter undergoing nonlinear dendritic processing.

- Neuronal regulation is a vital mechanism for counteracting the formation of pathologic attractors and for achieving long-term memory maintenance. While it is conceivable that unlearning may also serve to efficiently counteract the formation of pathologic attractors, it cannot cope with the problem of synaptic turnover and cannot act as a memory maintenance mechanism.
- Computationally, there is an important advantage to using NR rather than anti-Hebbian synaptic unlearning: The NR mechanism regulates itself, unlike unlearning that needs an external agent to turn it off after a certain optimal number of unlearning cycles.

- Biologically, while there is a rising body of recent experimental evidence testifying that NR takes place in both the peripheral and central nervous systems, the experimental support for unlearning has been fairly scarce. Correct timing is very important for Hebbian learning, as pointed out by van Hemmen[1], but its relation to unlearning remains to be studied.
- Unlearning has the advantage that it is able to increase the memory capacity of the intact network, while NR mainly works to preserve the existing capacity of a network undergoing synaptic turnover and degradation. Hence, the possibility that both mechanisms may exist should not be ruled out.

6 Discussion

The different facets of neuronal regulation extend over different time periods. The basic NR mechanism of Section 2 occurs both in the developing brain as well as in the mature brain over daily periods. We propose a more specific realization of it in the brain in the next few paragraphs. Development over periods of years fits into the description of long term maintenance of Section 3, where the original synaptic efficacies are no longer maintained and the stronger synapses survive. Finally, aging brings with it the phenomenon of synaptic deletion, which can be coped with provided the potential for NR is there and the system has not yet reached its critical capacity. Otherwise dementia will follow, as described in Section 4. Neuronal regulation hence presents an attractive and quite unique opportunity to address a broad range of normal and altered memory-related cognitive functioning within a common, simple framework.

Neuronal regulation relies on activation of the memory system by random inputs, thus testing all basins of attraction without requiring the explicit knowledge of the memory patterns themselves. For this purpose we use the same approach that was employed in the works [3, 4] that suggested the unlearning mechanisms. Such random activation of cortical memory systems may be triggered by PGO waves[30] during REM sleep, raising the possibility that NR takes place during sleep. NR is therefore a possible realization of 'dynamic stabilization', a term that describes the idea that during sleep there exist dynamic processes that maintain synaptic efficacies[12]. Note that in our approach we have to segment between Hebbian learning and neuronal regulation. The two processes, although being complementary, cannot take place simultaneously. This segregation seems to fit nicely with the existence of different stages of sleep that may thus subserve both memory consolidation and neuronal regulation. The triggering of one process or the other may be caused by the different neuromodulators that are dominant in different stages of sleep[31].

NR is a corrective procedure. As such it is advantageous to perform it quite often and in small doses. This way it is possible to intertwine learning of new memories and regulation of the whole system in an efficient manner[7]. Hence there is an advantage to invoking a regular periodic mechanism to implement NR, which is another reason to think of sleep, with its alternating phases of REM and non-REM sleep, as the suitable means for subserving this process.

Further experimental studies are needed to evaluate how the findings of Turrigiano *et al.* [11] of NR in the developmental stage carry on to adults. However, the instrumental potential of NR in obtaining memory maintenance, coupled with morphometric evidence showing that the average total synaptic area per unit volume is maintained throughout normal aging[32, 18], make it highly likely that NR plays an important functional role in adulthood too.

In summary, we conclude that neuronal regulation is a natural and plausible candidate for performing homeostasis of memory systems. Its common feature with unlearning is that it reduces basins of attraction that are too large, a very important property for keeping memory systems well balanced. It replaces synaptic unlearning by a neuronal based process, that complements Hebbian synaptic learning. Hebbian learning and neuronal regulation can occur in a segmented and intertwined fashion, relying on different modes of activation of the brain. They can go on without end, which is suitable for describing human life long processes.

References

- J.L. van Hemmen. Hebbian learning, its correlation catastrophe, and unlearning. Network, Comput. Neural Syst., 8:V1-V17, 1997.
- [2] J.J. Hopfield. Neural networks and physical systems with emergent collective abilities.
 Proc. Nat. Acad. Sci. USA, 79:2554, 1982.
- [3] F. Crick and G. Mitchison. The function of dream sleep. Nature, 304:111-114, 1983.
- [4] J.J. Hopfield, D.I. Feinstein, and R.G. Palmer. 'unlearning' has a stabilizing effect in collective memories. *Nature*, 304:158-159, 1983.
- [5] D. Horn and E. Ruppin. Compensatory mechanisms in an attractor neural network model of schizophrenia. Neural Computation, 7(1):182-205, 1995.
- [6] E. Ruppin, J. Reggia, and D. Horn. A neural model of positive schizophrenic symptoms. Schizophrenia Bulletin, 22(1):105-123, 1996.
- [7] D. Horn, N. Levy, and E. Ruppin. Neuronal homeostasis and memory maintenance. Neural Computation, 10:1–18, 1998.
- [8] G. LeMasson, E. Marder, and L.F. Abbott. Activity-dependent regulation of conductances in model neurons. *Science*, 259:1915–1917, 1993.
- [9] L.F. Abbott and G. LeMasson. Analysis of neuron models with dynamically regulated conductances. *Neural Computation*, 5:823-842, 1993.

- [10] A. van Ooyen. Activity-dependent neural network development. Network, 5:401-423, 1994.
- [11] G. G. Turrigiano, K. R. Leslie, N. S. Desai, L. C. Rutherford, and S. B. Nelson. Activitydependent scaling of quantal amplitude in neocortical neurons. *Nature*, 391:892-895, 1998.
- [12] J. L. Kavanau. Sleep and dynamic stabilization of neural circuitry: a review and synthesis. Behavioural Brain Research, 63:111-126, 1994.
- [13] M. V. Tsodyks. Associative memory in neural networks with the hebbian learning rule.
 Modern Physics Letters B, 3(7):555-560, 1989.
- [14] G. W. Davis and C. S. Goodman. Synapse-specific control of synaptic efficacy at the terminals of a single neuron. *Nature*, 392:82-86, 1998.
- [15] H. Coleman, J. Nabekura, and J. W. Lichtman. Alterations in synaptic strength preceding axon withdrawal. Science, 275:356-361, 1997.
- [16] H. Sompolinsky. The theory of neural networks: The hebb rule and beyond. In J. L. van Hemmen and I. Morgenstern, editors, *Heidelberg Colloquium on Glassy Dynamics*, pages 485-527. Springer Verlag, 1986.
- [17] G. Chechick, I. Meilijson, and E. Ruppin. Synaptic pruning in development: A novel account in neural terms. *Neural Computation*, 1998. to appear.
- [18] C. Bertoni-Freddari, P. Fattoretti, T. Casoli, W. Meier-Ruge, and J. Ulrich. Morphological adaptive response of the synaptic junctional zones in the human dentate gyrus during aging and alzheimer's disease. *Brain Research*, 517:69-75, 1990.
- [19] S. T. DeKosky and S.W. Scheff. Synapse loss in frontal cortex biopsies in alzheimer's disease: Correlation with cognitive severity. Ann. Neurology, 27(5):457-464, 1990.

- [20] S.W. Scheff, D.L. Sparks, and D.A. Price. Synapse loss in the temporal lobe in Alzheimer's disease. Annals of Neurology, 33:190-199, 1993.
- [21] R. D. Terry, E. Masliah, D. P. Salmon, N. Butters, R. DeTeresa, R. Hill, L. A. Hansen, and R. Katzman. Physical basis of cognitive alterations in Alzheimer's disease: Synapse loss is the major correlate of cognitive impairment. Ann. Neurology, 30:572-580, 1991.
- [22] E. Masliah, M. Mallory, L. Hansen, R. DeTeresa, M. Alford, and R. Terry. Synaptic and neuritic alterations during the progression of Alzheimer's disease. *Neuroscience Letters*, 174:67–72, 1994.
- [23] E. Masliah and R. Terry. The role of synaptic pathology in the mechanisms of dementia in alzheimer's disease. *Clinical Neuroscience*, 1:192–198, 1994.
- [24] D. Horn, N. Levy, and E. Ruppin. Neuronal-based synaptic compensation: A computational study in alzheimer's disease. *Neural Computation*, 8:1227 – 1243, 1996.
- [25] D. Horn, E. Ruppin, M. Usher, and M. Herrmann. Neural network modeling of memory deterioration in alzheimer's disease. *Neural Computation*, 5:736-749, 1993.
- [26] C.W. Cotman and K.J. Anderson. Synaptic plasticity and functional stabilization in the hippocampal formation: Possible role in alzheimer's disease. Adv. Neurol., 47:313-336, 1988.
- [27] C.W. Cotman and K.J. Anderson. Neural plasticity and regeneration. In G.J. Siegel et. al., editor, *Basic Neurochemistry: Molecular, cellular and medical aspects*, pages 507-522. Raven Press, 1989.
- [28] J.R. Stevens. Abnormal reinnervation as a basis for schizophrenia: A hypothesis. Arch. Gen. Psychiatry, 49:238-243, 1992.

- [29] N. Levy, D. Horn, and E. Ruppin. Associative memory in a multi-modular network. preprint, 1998.
- [30] J.A. Hobson and R.W. McCarley. The brain as a dream state generator: an activationsynthesis hypothesis of the dream process. *American Journal of Psychiatry*, 134:1335– 1368, 1977.
- [31] J. Allan Hobson. The Dreaming Brain. Harper Collins, 1988.
- [32] C. Bertoni-Freddari, W. Meier-Ruge, and J. Ulrich. Quantitative morphology of synaptic plasticity in the aging brain. Scanning Microsc., 2:1027-1034, 1988.