Weak Memory Concurrency in C/C++11

Ori Lahav



Haifa::C++ meeting November 21, 2017

```
Initially, x = y = 0.

x := 1; y := 1; b := x; if (a = 0) then /* critical section */ /* critical section */
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Is it safe?

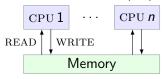
```
Initially, x = y = 0.

x := 1; y := 1; b := x; \# 0

if (a = 0) then f(b = 0) then
```

Is it safe?

Yes, if we assume sequential consistency (SC):



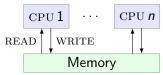
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Is it safe?

Yes, if we assume sequential consistency (SC):



No existing hardware implements SC!

- ► SC is very expensive (memory ~100 times slower than CPU).
- SC does not scale to many processors.

Example: Shared-memory concurrency in C++

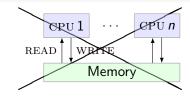
```
int X, Y, a, b;
void thread1() {
    X = 1;
    a = Y;
}
void thread2() {
    Y = 1;
    b = X;
}
```

```
int main () {
    int cnt = 0;
    do {
        X = 0: Y = 0:
        thread first(thread1);
        thread second(thread2):
        first.join();
        second.join();
        cnt++;
    } while (a != 0 || b != 0);
    printf("%d\n",cnt);
    return 0;
```

Example: Shared-memory concurrency in C++

```
int X, Y, a, b;
                              int main () {
                                   int cnt = 0;
     void thread1() {
                                  do {
         X = 1;
                                       X = 0: Y = 0:
         a = Y:
                                       thread first(thread1);
     void thread2() {
                                       thread second(thread2):
         Y = 1:
                                       first.join();
         b = X:
                                       second.join();
                                       cnt++;
If Dekker's mutual exclusion
                                 →} while (a != 0 || b != 0);
 is safe, this program will
                                   printf("%d\n",cnt);
      not terminate
                                   return 0:
```

Weak memory models



We look for a substitute for SC:

Unambiguous specification

▶ What are the possible outcomes of a multithreaded program?

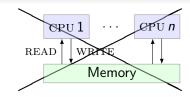
Typically called a weak memory model (WMM)

Allows more behaviors than SC.

Amenable to formal reasoning

Can prove theorems about the model.

Weak memory models



We look for a substitute for SC:

Unambiguous specification

▶ What are the possible outcomes of a multithreaded program?

Typically called a weak memory model (WMM)

Allows more behaviors than SC.

Amenable to formal reasoning

Can prove theorems about the model.

But it is not easy to get right

- ▶ The Java memory model is flawed.
- ▶ The C/C++11 model is also flawed.

The Problem of Programming Language Concurrency Semantics

Mark Batty, Kayvan Memarian, Kyndylan Nienhuis, Jean Pichon-Pharabod, and Peter Sewell

University of Cambridge

"Disturbingly, 40+ years after the first relaxed-memory hardware was introduced (the IBM 370/158MP), the field still *does not have a credible proposal for the concurrency semantics* of any general-purpose high-level language that includes high performance shared-memory concurrency primitives. This is a *major open problem* for programming language semantics."

European Symposium on Programming (ESOP) 2015

Plan for rest of the talk

- 1. Challenges for memory models
- 2. The C/C++11 memory model
- 3. The "out-of-thin-air" problem
- 4. A solution: a promising semantics

Plan for rest of the talk

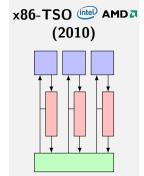
- 1. Challenges for memory models
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- 4. A solution: a promising semantics

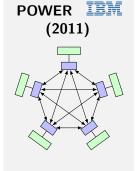
Challenge 1: Various hardware models

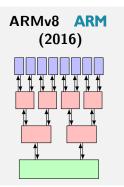


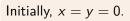










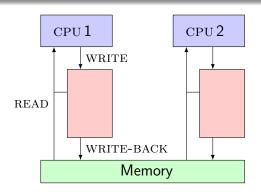


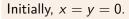
$$x := 1;$$

$$a := y; \ /\!\!/ 0$$

$$y := 1;$$

$$b := x; // 0$$



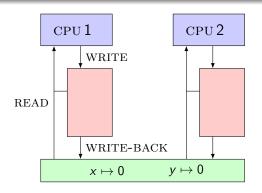


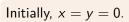


$$a := y; // 0$$

$$\triangleright$$
 $y := 1;$

$$b := x; // 0$$



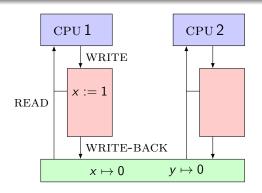


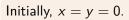


► a := y; // 0

$$\triangleright$$
 $y := 1;$

b := x; // 0



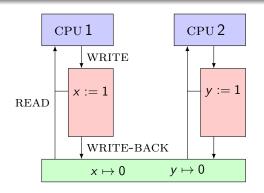


$$x := 1$$
;

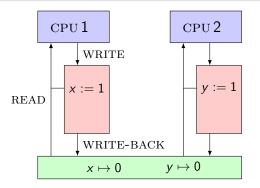
►
$$a := y$$
; // 0

$$y := 1;$$

▶ b := x; // 0



```
Initially, x=y=0.  \begin{aligned} x &:= 1; & & y &:= 1; \\ & \textbf{fence}; & & \textbf{fence}; \\ & a &:= y; \ /\!\!/ \ 0 & & b &:= x; \ /\!\!/ \ 0 \end{aligned}
```

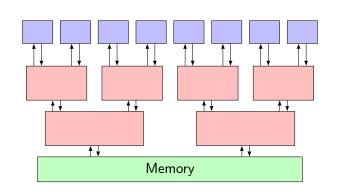




```
Initially, x = y = 0.
```

$$a := x; \ /\!\!/ 1$$

$$a := x; \ // 1$$
 $b := y; \ // 1$ $y := 1;$ $x := b;$

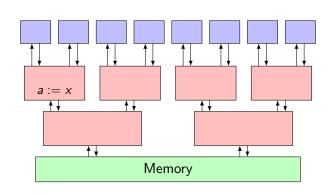




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Initially, x = y = 0.
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$$a := x; // 1$$

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 $b := y; \ // 1$ $y := 1;$ $x := b;$

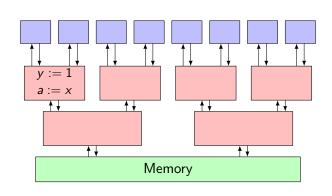




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Initially, x = y = 0.
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$$a := x; \ /\!\!/ 1$$

$$a := x; //1$$
 $b := y; //1$ $y := 1;$ $x := b;$

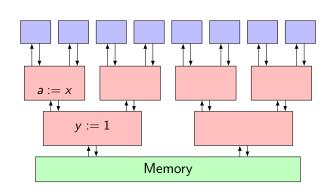




```
Initially, x = y = 0.
```

$$a := x; // 1$$

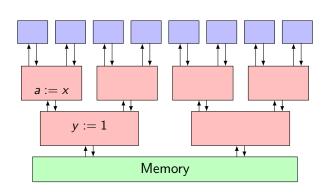
$$a := x; //1$$
 $b := y; //1$ $y := 1;$ $x := b;$





Initially,
$$x = y = 0$$
.

$$a := x; \ /\!\!/ 1$$
 $b := y; \ /\!\!/ 1$ $y := 1;$ $x := b;$



Challenge 2: Compilers stir the pot

Initially,
$$x = y = 0$$
.

$$x := 1;$$
 $b := x;$ $b := y;$ 1 $c := x;$ 0

forbidden under SC

Challenge 2: Compilers stir the pot

Initially,
$$x = y = 0$$
.

$$x := 1; \begin{vmatrix} a := x; \\ b := y; \ // 1 \\ c := x; \ // 0 \end{vmatrix}$$
 $x := 1; \begin{vmatrix} a := x; \\ b := y; \ // 1 \\ c := a; \ // 0 \end{vmatrix}$
 $x := 1; \begin{vmatrix} a := x; \\ b := y; \ // 1 \\ c := a; \ // 0 \end{vmatrix}$
 $x := 1; \begin{vmatrix} a := x; \\ b := y; \ // 1 \\ c := a; \ // 0 \end{vmatrix}$
 $x := 1; \begin{vmatrix} a := x; \\ b := y; \ // 1 \\ c := a; \ // 0 \end{vmatrix}$

A forbidden under SC

Challenge 3: Transformations do not suffice

Program transformations fail short to explain some weak behaviors:

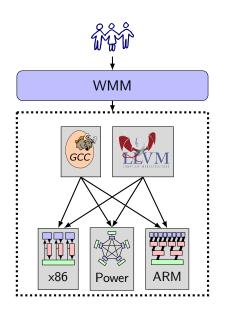
Message passing (MP) $x := 1; \quad || \quad a := y; \quad || \quad 1$ $y := 1; \quad || \quad b := x; \quad || \quad 0$

Independent reads of independent writes (IRIW)

$$a := x; \ // 1 \ b := y; \ // 0 \ || \ x := 1; \ || \ y := 1; \ || \ c := y; \ // 1 \ d := x; \ // 0$$

ARM-weak
$$a := x; \ /\!\!/ 1 \ | \ y := x; \ /\!\!/ 1 \ | \ x := y; \ /\!\!/ 1$$

Overview



WMM desiderata

- 1. Formal and comprehensive
- Not too weak (good for programmers)
- 3. Not too strong (good for hardware)
- 4. Admits optimizations (good for compilers)

The C11 memory model

- ▶ Introduced by the ISO C/C++ 2011 standards.
- ▶ Defines the semantics of concurrent memory accesses.

The C11 memory model: Atomics

Two types of accesses

Ordinary (Non-Atomic)

Races are errors

Atomic

Welcome to the expert mode

The C11 memory model: Atomics

Two types of accesses

Ordinary (Non-Atomic)

Races are errors

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Welcome to the expert mode

DRF (data race freedom) guarantee

 $\begin{array}{c} \text{no data races} \\ \text{under SC} \end{array} \Longrightarrow \begin{array}{c} \text{only} \\ \text{SC behaviors} \end{array}$

A spectrum of access modes

```
memory_order_seq_cst
                          (sc)
                     full memory fence
memory_order_release
                                memory_order_acquire
      write (rel)
                                       read (acq)
no fence (x86); Iwsync (PPC)
                                no fence (x86); isync (PPC)
                memory_order_relaxed
                         (rlx)
                         no fence
                    Non-atomic (na)
                 no fence, races are errors
```

+ Explicit primitives for fences

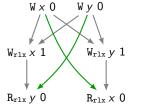
C11: a declarative memory model

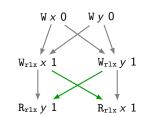
Declarative semantics abstracts away from implementation details.

- 1. a program \sim a set of directed graphs (called: *execution graphs*)
- 2. The memory model defines what executions are *consistent*.
- 3. The semantics of a program is the set of its consistent executions.
- 4. C/C++11 also has *catch-fire* semantics (i.e., forbidden data races).

Execution graphs

Store buffering (SB)





Relations

- Program order, po
- ▶ Reads-from, rf

C/C++11 formal model

[Vafeiadis & Narayan OOPSLA'13]

```
[-]: CExp \rightarrow \mathbb{P}((res : Val \cup \{\bot\}, A : \mathbb{P}(AName), lab : A \rightarrow Act, sb : \mathbb{P}(A \times A), fst : A, lst : A))
                                   [v] \stackrel{\text{def}}{=} \{ \langle v, \{a\}, \mathsf{lab}, \emptyset, a, a \rangle \mid a \in \mathsf{AName} \land \mathsf{lab}(a) = \mathsf{skip} \}
                       [alloc()] \stackrel{\text{def}}{=} \{ \langle \ell, \{a\}, lab, \emptyset, a, a \rangle \mid a \in AName \land \ell \in Loc \land lab(a) = A(\ell) \}
                  [\![v]_Z := v']\!] \stackrel{\text{def}}{=} \{\langle v', \{a\}, \mathsf{lab}, \emptyset, a, a \rangle \mid a \in \mathsf{AName} \land \mathsf{lab}(a) = W_Z(v, v')\}
                             ||[v]||_{\mathbb{Z}} \stackrel{\text{def}}{=} \{\langle v', \{a\}, | \mathsf{lab}, \emptyset, a, a \rangle \mid a \in \mathsf{AName} \land v' \in \mathsf{Val} \land |\mathsf{lab}(a) = \mathsf{R}_{\mathcal{Z}}(v, v')\}
 \begin{aligned} & \| \mathbf{CAS}_{X,Y}(v, v_o, v_n) \| \overset{\text{def}}{=} \left\{ \langle v', \{a\}, \mathsf{lab}, \emptyset, a, a \rangle \mid a \in \mathsf{AName} \land v' \in \mathsf{Val} \land v' \neq v_o \land \mathsf{lab}(a) = \mathrm{R}_Y(v, v') \right\} \\ & \cup \left\{ \langle v_o, \{a\}, \mathsf{lab}, \emptyset, a, a \rangle \mid a \in \mathsf{AName} \land \mathsf{lab}(a) = \mathrm{RMW}_X(v, v_o, v_n) \right\} \end{aligned} 
    \| \mathbf{let} \ x = E_1 \ \mathbf{in} \ E_2 \| \stackrel{\text{def}}{=} \{ \langle \bot, A_1, | \mathbf{ab_1}, \mathbf{sb_1}, fst_1, lst_1 \rangle \mid \langle \bot, A_1, | \mathbf{ab_1}, \mathbf{sb_1}, fst_1, lst_1 \rangle \in \| E_1 \| \}
                                            \cup {\langle res_2, A_1 \uplus A_2, lab_1 \cup lab_2, sb_1 \cup sb_2 \cup \{(lst_1, fst_2)\}, fst_1, lst_2 \rangle
                                                   (v_1, A_1, \mathsf{lab}_1, \mathsf{sb}_1, fst_1, lst_1) \in [\![E_1]\!] \land (res_2, A_2, \mathsf{lab}_2, \mathsf{sb}_2, fst_2, lst_2) \in [\![E_2[v_1/x]]\!] \}
        \llbracket \mathbf{repeat} \ E \ \mathbf{end} \rrbracket \stackrel{\mathrm{def}}{=} \{\langle res_N, \biguplus_{i \in [1..N]} \mathcal{A}_i, \bigcup_{i \in [1..N]} \mathsf{lab}_i, \bigcup_{i \in [1..N]} \mathsf{sb}_i \cup \{(lst_1, fst_2), \dots, (lst_{N-1}, fst_N)\}, fst_1, lst_N \rangle \mid \mathsf{frace} \rbrace \}
                                                     \forall i. \langle res_i, A_i, lab_i, sb_i, fst_i, lst_i \rangle \in |E| \land (i \neq N \implies res_i = 0) \land res_N \neq 0 
                        \llbracket E_1 \rrbracket E_2 \rrbracket \stackrel{\mathrm{def}}{=} \{ (\mathsf{combine}(res_1, res_2), \mathcal{A}_1 \uplus \mathcal{A}_2 \uplus \{ a_{\mathsf{fork}}, a_{\mathsf{ioin}} \}, \mathsf{lab}_1 \cup \mathsf{lab}_2 \cup \{ a_{\mathsf{fork}} \mapsto \mathsf{skip}, a_{\mathsf{ioin}} \mapsto \mathsf{skip} \},
                                                      sb_1 \cup sb_2 \cup \{(a_{fork}, fst_1), (a_{fork}, fst_2), (lst_1, a_{join}), (lst_2, a_{join})\}, a_{fork}, a_{join}\}
                                                    (res_1, A_1, sb_1, fst_1, lst_1) \in [E_1] \land (res_2, A_2, sb_2, fst_2, lst_2) \in [E_2] \land a_{fork}, a_{loin} \in AName
                                                                     Figure 2. Semantics of closed program expressions.
                                                                                                           \exists x \ \mathsf{hb}(x \ x)
                                                                                                                                                                                                                 (IrreflexiveHB)
                                                                  \forall \ell. totalorder(\{a \in A \mid iswrite_{\ell}(a)\}, mo) \land hb_{\ell} \subseteq mo
                                                                                                                                                                                                               (ConsistentMO)
                                     totalorder(\{a \in A \mid isSeqCst(a)\}, sc) \land hb_{SeqCst} \subseteq sc \land mo_{SeqCst} \subseteq sc
                                                                                                                                                                                                                 (ConsistentSC)
                                        \forall b. \ rf(b) \neq \bot \iff \exists \ell, a. \ iswrite_{\ell}(a) \land isread_{\ell}(b) \land hb(a, b)
                                                                                                                                                                                                        (Consistent REdom)
                                       \forall a, b. \ rf(b) = a \implies \exists \ell, v. \ iswrite_{\ell,v}(a) \land isread_{\ell,v}(b) \land \neg hb(b, a)
                                                                                                                                                                                                                 (ConsistentRE)
                                     \forall a, b, \text{ rf}(b) = a \land (\text{mode}(a) = \text{na} \lor \text{mode}(b) = \text{na}) \implies \text{hb}(a, b)
                                                                                                                                                                                                            (ConsistentRFna)
               \forall a, b. \ \mathsf{rf}(b) = a \land \mathsf{isSeqCst}(b) \implies \mathsf{isc}(a, b) \lor \neg \mathsf{isSeqCst}(a) \land (\forall x. \ \mathsf{isc}(x, b) \Rightarrow \neg \mathsf{hb}(a, x))
                                                                                                                                                                                                               (RestrSCReads)
                                                                    \nexists a, b. \ \mathsf{hb}(a, b) \land \mathsf{mo}(\mathsf{rf}(b), \mathsf{rf}(a)) \land \mathsf{locs}(a) = \mathsf{locs}(b)
                                                                                                                                                                                                                   (CoherentRR)
                                                           \exists a, b, hb(a, b) \land mo(rf(b), a) \land iswrite(a) \land locs(a) = locs(b)
                                                                                                                                                                                                                 (CoherentWR)
                                                           \nexists a, b. \ hb(a, b) \land mo(b, rf(a)) \land iswrite(b) \land locs(a) = locs(b)
                                                                                                                                                                                                                 (CoherentRW)
                                \forall a. \text{ isrmw}(a) \land \text{rf}(a) \neq \bot \implies \text{mo}(\text{rf}(a), a) \land \nexists c. \text{mo}(\text{rf}(a), c) \land \text{mo}(c, a)
                                                                                                                                                                                                                 (AtomicRMW)
                                                                            \forall a, b, \ell, \ \mathsf{lab}(a) = \mathsf{lab}(b) = \mathsf{A}(\ell) \implies a = b
                                                                                                                                                                                                            (ConsistentAlloc)
where \mathsf{iswrite}_{\ell,v}(a) \stackrel{\text{def}}{=} \exists X, v_{\text{old}}.\ \mathsf{lab}(a) \in \{W_X(\ell,v), RMW_X(\ell,v_{\text{old}},v)\}
                                                                                                                                                      iswrite_{\ell}(a) \stackrel{\text{def}}{=} \exists v. iswrite_{\ell,v}(a)
              isread_{\ell,v}(a) \stackrel{\text{def}}{=} \exists X, v_{\text{new}}. lab(a) \in \{R_X(\ell, v), RMW_X(\ell, v, v_{\text{new}})\}
             rsElem(a, b) \stackrel{\text{def}}{=} sameThread(a, b) \lor isrmw(b)
                      rseq(a) \stackrel{\text{def}}{=} \{a\} \cup \{b \mid rsElem(a,b) \land mo(a,b) \land (\forall c. mo(a,c) \land mo(c,b) \Rightarrow rsElem(a,c))\}
                               sw \stackrel{\text{def}}{=} \{(a,b) \mid \mathsf{mode}(a) \in \{\mathsf{rel.\,rel\,acq.\,sc}\} \land \mathsf{mode}(b) \in \{\mathsf{acq.\,rel\,acq.\,sc}\} \land \mathsf{rf}(b) \in \mathsf{rseq}(a)\}
                                hb \stackrel{\text{def}}{=} (sb \cup sw)^+
                             \mathsf{hb}_{\ell} \stackrel{\mathrm{def}}{=} \{(a, b) \in \mathsf{hb} \mid \mathsf{iswrite}_{\ell}(a) \land \mathsf{iswrite}_{\ell}(b)\}
                      X_{SeqCst} \stackrel{\text{def}}{=} \{(a, b) \in X \mid isSeqCst(a) \land isSeqCst(b)\}
                     isc(a, b) \stackrel{\text{def}}{=} iswrite_{locs(b)}(a) \land sc(a, b) \land \nexists c. sc(a, c) \land sc(c, b) \land iswrite_{locs(b)}(c)
                                Figure 3. Axioms satisfied by consistent C11 executions. Consistent (A, lab. sb. rf. mo. sc).
       c: W(\ell, 1) \longrightarrow a: R(\ell, 1) \mid c: W(\ell, 2) \xrightarrow{ma} a: W(\ell, 1) \mid c: W(\ell, 1) \xrightarrow{d} a: R(\ell, 1)
                 1 mo
                                         ыЫ
       d: W(\ell, 2) \longrightarrow b: R(\ell, 2)
            violates Coherent RR
                                                                  violates CoherentWR
```

Basic ingredients of execution graph consistency

- 1. SC-per-location (a.k.a. coherence)
- 2. Release/acquire synchronization
- 3. Global conditions on SC accesses

Basic ingredients of execution graph consistency

- 1. SC-per-location (a.k.a. coherence)
- 2. Release/acquire synchronization
- 3. Global conditions on SC accesses

SC-per-location

Definition (Declarative definition of SC)

G is SC-consistent if there exists a relation sc s.t. the following hold:

- sc is a total order on the events of G.
- ▶ If po∪rf ⊂ sc.
- ▶ If $\langle a, b \rangle \in \text{rf}$ then there does not exist $c \in \mathbb{W}_{\text{loc}(a)}$ such that $\langle a, c \rangle \in \text{sc}$ and $\langle c, b \rangle \in \text{sc}$.

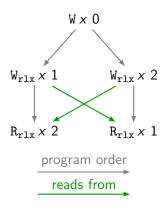
Definition (SC-per-location)

G is satisfies *SC-per-location* if for every location x, there exists a relation sc_x s.t. the following hold:

- ightharpoonup sc_x is a total order on the events of G that access x.
- ▶ If po \cup rf \subseteq sc_x.
- ▶ If $\langle a, b \rangle \in \text{rf}$ then there does not exist $c \in W_x$ such that $\langle a, c \rangle \in \text{sc}_x$ and $\langle c, b \rangle \in \text{sc}_x$.

SC-per-location: Example

$$\begin{aligned} x &= 0 \\ x &:=_{\mathtt{rlx}} 1 & x :=_{\mathtt{rlx}} 2 \\ a &:= x_{\mathtt{rlx}} & b := x_{\mathtt{rlx}} \end{aligned}$$



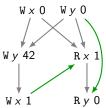
inconsistent!

Release/acquire synchronization

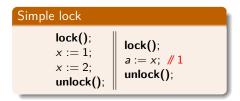
SC-per-location is often too weak:

▶ It does not support the message passing idiom:

```
Message passing (MP)
y := 42; \quad || \quad a := x; \ // 1 \\ x := 1; \quad || \quad b := y; \ // 0
```



▶ We cannot even implement locks:



```
int y = 0;
int x = 0;
y = 42; || if(x == 1){
x = 1; || print(y);
```

```
int y = 0;
int x = 0;
y = 42; || if(x == 1){
x = 1; || print(y);
```

```
int y = 0;
int x = 0;
y = 42; | if(x == 1){
x = 1; | race | print(y);
}
```

```
int y = 0;
 int x = 0;
```

```
int y = 0;
                                                atomic < int > x = 0;
y = 42; | if(x == 1){

x = 1; | race | print(y); | x =<sub>rlx</sub> 1; | print(y); | }
```

```
int y = 0;
int x = 0;
```

```
int y = 0;
                                                     atomic < int > x = 0;
y = 42; if (x == 1) { y = 42; if (x_{rlx} == 1) { x = 1; race print(y); } x =_{rlx} 1; race print(y);
```

```
int y = 0;
 int x = 0;
```

```
int y = 0;
                                                   atomic<int> x = 0;
y = 42; if (x == 1) { y = 42; if (x_{rlx} == 1) { x = 1; race print(y); x =_{rlx} 1; race print(y);
```

```
int y = 0;
     atomic<int> x = 0;
y = 42;  || if(x<sub>acq</sub> == 1){
x =<sub>rel</sub> 1;  || print(y);
```

```
int y = 0;
 int x = 0;
```

```
int y = 0;
                                                   atomic<int> x = 0;
y = 42; if (x == 1) { y = 42; if (x_{rlx} == 1) { x = 1; race print(y); x =_{rlx} 1; race print(y);
```

```
int y = 0;
     atomic<int> x = 0;
y = 42; if (x<sub>acq</sub> == 1) {
x = rel 1; print(y);
```

```
int y = 0;
 int x = 0;
```

```
int y = 0;
                                                   atomic<int> x = 0;
y = 42; if (x == 1) { y = 42; if (x_{rlx} == 1) { x = 1; race print(y); x =_{rlx} 1; race print(y);
```

```
int y = 0;
     atomic<int> x = 0;
y = 42; | if(x<sub>acq</sub> == 1){
x = rel 1 | sw print(y);
```

```
int y = 0;
 int x = 0;
```

```
int y = 0;
                                              atomic<int> x = 0;
y = 42; if (x == 1) { y = 42; if (x_{rlx} == 1) { x = 1; race print(y); x =_{rlx} 1; race print(y);
```

```
int y = 0;
    atomic<int> x = 0;
y = 42; | if(x<sub>acq</sub> == 1){
x =<sub>rel</sub> 1 | print(y);
}
```

```
int y = 0;
   atomic<int> x = 0;
y = 42;
fence<sub>rel</sub>;
x =<sub>rlx</sub> 1; if(x<sub>rlx</sub> == 1){
    fence<sub>acq</sub>;
    print(y);
}
```

```
int y = 0;
 int x = 0;
```

```
int y = 0;
                                  atomic<int> x = 0;
y = 42; if (x == 1) { y = 42; if (x_{rlx} == 1) { x = 1; race print(y); x =_{rlx} 1; race print(y);
```

```
int y = 0;
atomic<int> x = 0;
```

```
int y = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 atomic<int> x = 0;
y = 42; | if (x_{acq} == 1) { | y = 42; | if (x_{rlx} == 1) { | x =_{rel} 1 | x =_{rel} 1 | x =_{rlx} 1 | x =_
```

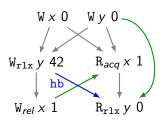
```
int y = 0;
 int x = 0;
```

```
int y = 0;
atomic<int> x = 0;
```

```
int y = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         atomic<int> x = 0;
y = 42; | if (x_{acq} == 1) { | y = 42; | if (x_{rlx} == 1) { | x =_{rel} = 1 | x =_{rel} = 1 | | x =_{rel} = 1
```

The "happens-before" relation

- ▶ hb should be acyclic.
- ► The SC-per-location orders should contain hb.
- Using acquire CAS's and release writes, we can implement locks.



SC accesses and fences

Store buffer

$$x := 1;$$

 $a := y;$ // 0 | $y := 1;$
 $b := x;$ // 0

How to guarantee only SC behaviors (i.e., $a = 1 \lor b = 1$)?

$$x :=_{sc} 1;$$
 $y :=_{sc} 1;$ $z :=_{rlx} 1;$

SC semantics

- Perhaps surprisingly, the semantics of SC atomics is the most complicated part of the model.
- ► C/C++11 provides too strong semantics (a correctness problem!)

In addition, its semantics for SC fences is too weak.

 \blacktriangleright Recently, the standard committee fixed the specification following: [Repairing Sequential Consistency in C/C++11 PLDI'17]

The "out-of-thin-air" problem

non-atomic

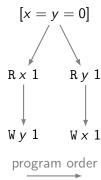
□ relaxed □ release/acquire □ sc

```
\verb|non-atomic| \qquad \boxed{\texttt{relaxed}} \qquad \boxed{} \qquad \boxed{
```

non-atomic □ (relaxed) □ release/acquire sc

Load-buffering

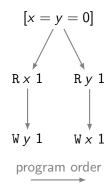
$$a := x; \ // 1$$
 $b := y; \ // 1$ $y := 1;$ $x := b;$



 $\verb|non-atomic| \qquad \boxed{\texttt{relaxed}} \qquad \boxed{} \qquad \verb|release/acquire| \qquad \boxed{} \qquad \verb|sc||$

Load-buffering

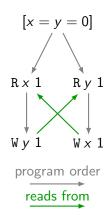
$$a := x; \ // 1$$
 $b := y; \ // 1$ $y := 1;$ $x := b;$



 $\verb|non-atomic| \qquad \boxed{\texttt{relaxed}} \quad \boxed{} \qquad \verb|release/acquire| \qquad \boxed{} \qquad \verb|sc||$

Load-buffering

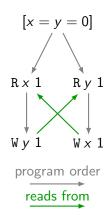
$$a := x; \ // 1$$
 $b := y; \ // 1$ $y := 1;$ $x := b;$



 $\verb|non-atomic| \qquad \boxed{\texttt{relaxed}} \quad \boxed{} \qquad \verb|release/acquire| \qquad \boxed{} \qquad \verb|sc||$

Load-buffering

$$a := x; \ // 1$$
 $b := y; \ // 1$ $y := 1;$ $x := b;$



relaxed non-atomic □ release/acquire sc

Load-buffering

$$a := x; //1$$

$$y:=1$$
;

$$x := b;$$

C/C++11 allows this behavior because POWER & ARM allow it!

Load-buffering + data dependency

$$a := x; // 1$$

 $y := a;$

$$b := y; // 1$$

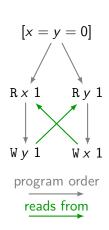
$$y := a$$

$$x := b$$
;

C/C++11 allows this behavior.

Values appear out-of-thin-air!

(no hardware/compiler exhibit this behavior)



 $\verb|non-atomic| \qquad \boxed{\texttt{relaxed}} \quad \boxed{} \qquad \verb|release/acquire| \qquad \boxed{} \qquad \verb|sc||$

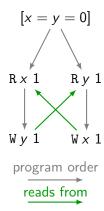
Load-buffering + control dependency

$$a := x; // 1$$

if $(a = 1)$
 $y := 1;$
 $b := y; // 1$
if $(b = 1)$
 $x := 1;$

 $\ensuremath{\text{C}/\text{C}}\xspace++11$ allows this behavior.

The DRF guarantee is broken!



$\mathsf{Load} ext{-}\mathsf{buffering} + \mathsf{control} \; \mathsf{dependency}$

$$a := x; // 1$$
if $(a = 1)$

$$b := y; // 1$$

if $(b = 1)$

$$\begin{bmatrix} x = y = 0 \end{bmatrix}$$

The three examples have the same execution graph!

The DRF guarantee is broken!

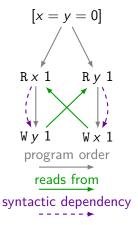


The hardware solution

Keep track of syntactic dependencies and forbid dependency cycles.

Load-buffering $a := x; \ // 1 \qquad \qquad | b := y; \ // 1 \qquad \qquad y := 1; \qquad | x := b;$

Load-buffering
$$+$$
 data dependency $a:=x; \ /\!\!/ 1 \qquad \qquad \parallel \quad b:=y; \ /\!\!/ 1 \ y:=a; \qquad \qquad \parallel \quad x:=b;$



The hardware solution

Keep track of syntactic dependencies and forbid dependency cycles.

Load-buffering

$$a := x : // 1$$

$$a := x; //1$$
 $b := y; //1$ $y := 1;$ $x := b;$

$$y := 1;$$

$$x := b$$
;

Load-buffering + data dependency

$$a := x \cdot // 1$$

$$a := x; \ // 1$$
 $b := y; \ // 1$ $y := a;$ $x := b;$

$$y := a;$$

$$a := x$$
; // 1

$$a := x; //1$$

 $y := a + 1 - a;$ $b := y; //1$
 $x := b;$

This approach is not suitable for a programming language: Compilers do not preserve syntactic dependencies.

The "out-of-thin-air" problem

- ► The C/C++11 model is too weak:
 - ▶ Values might appear *out-of-thin-air*.
 - ▶ The *DRF guarantee* is broken.

- A straightforward solution:
 - ▶ Disallow po Urf cycles
 - But, on weak hardware it carries a certain implementation cost.

Solving the problem without changing the compilation schemes will require a major revision of the standard.

A 'promising' solution to OOTA

[Jeehoon Kang, Chung-Kil Hur, Ori Lahav, Viktor Vafeiadis, Derek Dreyer POPL'17]

We propose a model that satisfies all WMM desiderata, and covers nearly all features of C11.

- ▶ No "out-of-thin-air" values
- Efficient h/w mappings

DRF guarantees

Compiler optimizations

Key idea: Start with an operational interleaving semantics, but allow threads to **promise** to write in the future.

Store-buffering $\begin{aligned} x &= y = 0 \\ x &= 1; & y &= 1; \\ a &= y; \ /\!\!/ \ 0 & b &= x; \ /\!\!/ \ 0 \end{aligned}$

Memory $\langle x:0@0\rangle$ $\langle y:0@0\rangle$

$$\frac{T_1 \text{'s view}}{\frac{x}{0}}$$

$$\frac{T_2\text{'s view}}{\begin{array}{cc} x & y \\ \hline 0 & 0 \end{array}$$

▶ Global memory is a pool of messages of the form

⟨location : value @ timestamp⟩

► Each thread maintains a *thread-local view* recording the last observed timestamp for every location

Store-buffering x = y = 0x = 1; b = x; # 0 b = x; # 0

Memory $\langle x:0@0\rangle$

$$\frac{T_2\text{'s view}}{\frac{x}{0}}$$

Global memory is a pool of messages of the form

(location : value @ timestamp)

► Each thread maintains a *thread-local view* recording the last observed timestamp for every location

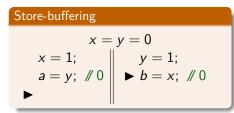
Memory $\langle x:0@0\rangle$ $\langle y:0@0\rangle$ $\langle x:1@1\rangle$ $\langle y:1@1\rangle$

$$T_1$$
's view $\frac{x}{x} = \frac{y}{0}$

$$\begin{array}{c|c}
T_2's \text{ view} \\
\hline
x & y \\
\hline
0 & X \\
\hline
1
\end{array}$$

Global memory is a pool of messages of the form

► Each thread maintains a *thread-local view* recording the last observed timestamp for every location



Memory $\langle x:0@0\rangle$ $\langle y:0@0\rangle$ $\langle x:1@1\rangle$ $\langle y:1@1\rangle$

$$T_1$$
's view
$$\begin{array}{cc} x & y \\ \hline & 0 \\ 1 \end{array}$$

Global memory is a pool of messages of the form

► Each thread maintains a *thread-local view* recording the last observed timestamp for every location

Store-buffering $\begin{aligned} x &= y = 0 \\ x &= 1; \\ a &= y; \ \# \ 0 \end{aligned} \quad \begin{aligned} y &= 1; \\ b &= x; \ \# \ 0 \end{aligned}$

Memory \(\langle x : 0@0\) \(\langle y : 0@0\) \(\langle x : 1@1\) \(\langle y : 1@1\)

$$T_1$$
's view $\begin{array}{c|c} X & y \\ \hline & 0 \\ 1 \end{array}$

$$\begin{array}{c|c}
T_2 \text{'s view} \\
\hline
x & y \\
\hline
0 & X \\
\hline
1
\end{array}$$

Global memory is a pool of messages of the form

► Each thread maintains a *thread-local view* recording the last observed timestamp for every location

Store-buffering

$$x = y = 0$$

 $x = 1;$ $y = 1;$ $b = x; // 0$

Memory

 $\langle x:0@0\rangle$ $\langle x: 1@1 \rangle$ $\langle y: 1@1 \rangle$

T_1 's view

$$T_2$$
's view x y

Coherence Test

$$x = 0$$

 $x := 1;$ $x := 2;$
 $a = x;$ $/\!\!/ 2$ $b = x;$ $/\!\!/ 1$

Store-buffering

$$x = y = 0$$

 $x = 1;$ $y = 1;$
 $a = y; \# 0$ $b = x; \# 0$

Memory

$$\langle x : 0@0 \rangle$$

 $\langle y : 0@0 \rangle$
 $\langle x : 1@1 \rangle$
 $\langle y : 1@1 \rangle$

$$T_1$$
's view

$$\begin{array}{c|c}
x & y \\
\hline
 & 0 & 0 \\
\hline
 & 1 & 1
\end{array}$$

$$T_2$$
's view X Y

Coherence Test

$$x = 0$$
 $x = 1;$
 $a = x; // 2$
 $x = 2;$
 $b = x; // 1$

Memory $\langle x:0@0\rangle$

$$T_1$$
's view $\frac{x}{0}$

$$T_2$$
's view

0

Store-buffering

$$x = y = 0$$

 $x = 1;$ $y = 1;$ $b = x; \# 0$

Memory

$$\langle x:0@0\rangle$$

 $\langle y:0@0\rangle$
 $\langle x:1@1\rangle$

 $\langle y: 1@1 \rangle$

$$T_1$$
's view

$$T_2$$
's view $\frac{x \quad y}{0}$

Coherence Test

Memory

$$\langle x:0@0\rangle$$

 $\langle x:1@1\rangle$

$$T_1$$
's view

$$T_2$$
's view

Store-buffering

$$x = y = 0$$

 $x = 1;$ $y = 1;$ $b = x;$ #0

Memory

$$\langle x : 0@0 \rangle$$

 $\langle y : 0@0 \rangle$
 $\langle x : 1@1 \rangle$
 $\langle y : 1@1 \rangle$

$$T_1$$
's view

$$T_2$$
's view $x \quad v$

Coherence Test

Memory

$$\langle x:0@0\rangle$$

 $\langle x:1@1\rangle$
 $\langle x:2@2\rangle$

$$T_1$$
's view $\frac{x}{x}$

$$T_2$$
's view $\frac{x}{x}$

Store-buffering

$$x = y = 0$$

 $x = 1;$ $y = 1;$ $b = x;$ #0

Memory

$$\langle x:0@0\rangle$$

 $\langle y:0@0\rangle$
 $\langle x:1@1\rangle$

 $\langle y: 1@1 \rangle$

$$T_1$$
's view

$$\begin{array}{c|c} x & y \\ \hline & 1 & \end{array} \qquad \begin{array}{c|c} x & y \\ \hline & 0 & \times \\ & 1 & \end{array}$$

$$T_2$$
's view

Coherence Test

$$x = 0$$

 $x := 1;$ $x := 2;$ $b = x;$ // 1

Memory

 $\langle x:0@0\rangle$ $\langle x:1@1\rangle$ $\langle x:2@2\rangle$

 T_1 's view

$$T_2$$
's view $\frac{x}{x}$

Store-buffering

$$x = y = 0$$

 $x = 1;$ $y = 1;$ $b = x;$ #0

Memory

 $\langle x:0@0\rangle$ $\langle y:0@0\rangle$ $\langle x: 1@1 \rangle$

 $\langle y: 1@1 \rangle$

$$T_1$$
's view

 $\begin{array}{c|c} x & y \\ \hline & x & y \\ \hline & 0 & \hline & 1 \\ \end{array}$

$$T_2$$
's view

Coherence Test

$$x = 0$$

 $x := 1;$ $x := 2;$ $b = x; // 1$

Memory

 $\langle x:0@0\rangle$ $\langle x:1@1\rangle$ $\langle x:2@2\rangle$

T_1 's view

T_2 's view

Load-buffering $a := x; \ /\!\!/ 1 \\ y := 1; \qquad x := y;$

- ► To model load-store reordering, we allow "promises".
- At any point, a thread may promise to write a message in the future, allowing other threads to read from the promised message.

Load-buffering

►
$$a := x; // 1$$

 $y := 1;$ ► $x := y;$

Memory

$$\langle x:0@0\rangle$$

 $\langle y:0@0\rangle$

$$T_1$$
's view $\frac{x}{0} = \frac{y}{0}$

$$T_2$$
's view $\frac{x}{0} = \frac{y}{0}$

- ► To model load-store reordering, we allow "promises".
- At any point, a thread may promise to write a message in the future, allowing other threads to read from the promised message.

Load-buffering

Memory $\langle x:0@0\rangle$

$$\frac{\langle y:0@0\rangle}{\langle y:1@1\rangle}$$

$$T_1$$
's view
$$\frac{x}{0} = \frac{y}{0}$$

$$\begin{array}{c|c}
T_2's \text{ view} \\
\hline
x & y \\
\hline
0 & 0
\end{array}$$

- ► To model load-store reordering, we allow "promises".
- At any point, a thread may promise to write a message in the future, allowing other threads to read from the promised message.

Load-buffering

Memory
$$\langle x:0@0\rangle$$
 $\langle y:0@0\rangle$

$$T_1$$
's view $\frac{x}{0} = \frac{y}{0}$

$$T_2$$
's view
$$\begin{array}{ccc} x & y \\ \hline 0 & \chi \\ & 1 \end{array}$$

- ► To model load-store reordering, we allow "promises".
- At any point, a thread may promise to write a message in the future, allowing other threads to read from the promised message.

Load-buffering

Memory

$$\langle x:0@0\rangle$$

 $\langle y:0@0\rangle$
 $\langle y:1@1\rangle$
 $\langle x:1@1\rangle$

 T_1 's view

 T_2 's view $\begin{array}{c|c} x & y \\ \hline & \chi & \chi \\ \hline & \chi & \chi \\ \hline & 1 & 1 \end{array}$

- ► To model load-store reordering, we allow "promises".
- At any point, a thread may promise to write a message in the future, allowing other threads to read from the promised message.

Load-buffering $a := x; \ // 1$ y := 1; x := y;

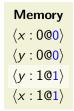
Memory
$$\langle x:0@0\rangle$$
 $\langle y:0@0\rangle$ $\langle y:1@1\rangle$ $\langle x:1@1\rangle$

$$T_1$$
's view $\begin{array}{c|c} x & y \\ \hline & 0 \\ 1 \end{array}$

$$T_2$$
's view
$$\begin{array}{c|c} x & y \\ \hline & \chi & \chi \\ \hline & 1 & 1 \end{array}$$

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Load-buffering

Memory

$$\langle x:0@0\rangle$$

 $\langle y:0@0\rangle$
 $\langle y:1@1\rangle$
 $\langle x:1@1\rangle$

$$T_1$$
's view $\frac{x}{x}$ $\frac{y}{x}$ $\frac{y}{x}$ $\frac{y}{x}$ $\frac{y}{x}$

$$T_2$$
's view
$$\begin{array}{c|c} x & y \\ \hline & X & X \\ \hline & 1 & 1 \end{array}$$

Load-buffering + dependency

$$a := x; //1 y := a;$$
 $x := y;$

Must not admit the same execution!

Load-buffering

${\sf Load\text{-}buffering} + {\sf dependency}$

$$a := x; //1 \ y := a;$$
 $x := y;$

Key Idea

A thread can only promise if it can perform the write anyway (even without having made the promise)

Certified promises

Thread-local certification

A thread can promise to write a message, if it can *thread-locally certify* that its promise will be fulfilled.

Certified promises

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Load-buffering

$$a := x; //1 y := 1;$$
 $x := y;$

Load buffering + fake dependency

$$a := x; //1$$

 $y := a + 1 - a;$ $x := y;$

 T_1 may promise y := 1, since it is able to write y := 1 by itself.

Load buffering + dependency

$$a := x; //1 y := a;$$
 $x := y;$

 T_1 may **NOT** promise y := 1, since it is not able to write y := 1 by itself.

Is this behavior possible?

$$a := x$$
; // 1

$$x := 1;$$

Is this behavior possible?

$$a := x; // 1$$

 $x := 1;$

No.

Suppose the thread promises x := 1. Then, once a := x reads 1, the thread view is increased and so the promise cannot be fulfilled.

Is this behavior possible?

$$a := x; \ /\!\!/ 1 \ | \ y := x; \ | \ x := y;$$

Is this behavior possible?

$$a := x; \ /\!\!/ 1 \ || \ y := x; \ || \ x := y;$$

Yes. And the ARM model allows it!

Is this behavior possible?

$$a := x; \ // 1 \ | \ y := x; \ | \ x := y;$$

Yes. And the ARM model allows it!

This behavior can be also explained by sequentialization:

$$a := x; \ // 1 \ | \ y := x; \ | \ x := y; \ \sim \ \begin{cases} a := x; \ // 1 \ x := y; \\ x := 1; \end{cases} \ | \ x := y; \ | \ x := y;$$

The full model (POPL'17)

We have extended this basic idea to handle:

- Atomic updates (e.g., CAS, fetch-and-add)
- ► Release/acquire fences and accesses
- Release sequences
- SC fences
- ▶ Plain accesses (C11's non-atomics & Java's normal accesses)

Results

- No "out-of-thin-air" values
- DRF guarantees
- Efficient h/w mappings (x86-TSO, Power, ARM)
- ► Compiler optimizations (incl. reorderings, eliminations)

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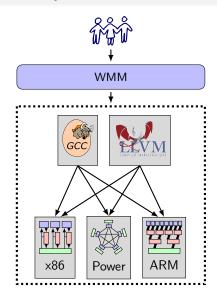
The **Coq** proof assistant



Results

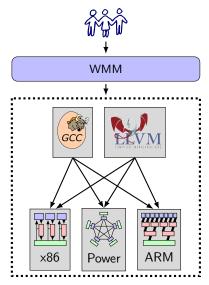
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Summary



- ► The challenges in designing a WMM.
- ► The C/C++11 model.
- ightharpoonup C/C++11 is broken:
 - Most problems are locally fixable.
 - But ruling out OOTA requires an entirely different approach.
- ► The **promising model** may be the solution.

Summary



- ► The challenges in designing a WMM.
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 - But ruling out OOTA requires an entirely different approach.
- ► The **promising model** may be the solution.

Thank you!

http://www.cs.tau.ac.il/~orilahav/